## LESSON PLAN

| Level | $:$ Senior High School |
| :--- | :--- |
| Lesson | $:$ Mathematics |
| Grade/Semester: $\mathrm{XI} / 1$ |  |
| Duration Time | $: 30$ Minutes |

## A.Standard Competence

Using statistics rules, counting rules, and characteristics of probability in problem solving.

## B. Basic Competence

Determining probability of an event.

## C. Indicators

1. Determining experimental probability of an event.
2. Determining theoretical probability of an event.

## Learning Objectives

1. Students are able to determine experimental probability of an event.
2. Students are able to determine theoretical probability of an event.

## Lesson Subject

Probability

## Learning Model

Learning model : Cooperative Learning

## Learning Steps

## a. Introduction

$1^{\text {st }}$ phase: Clarify the learning goals and motivate students.

1. Clarify the learning goals.
2. Facilitate students to remember the last lesson about counting rules, permutation, and combination.
3. Motivate students by relating this lesson to their daily activity.
Example:
When you toss pair of dice in a game, there are many possibility of the result. The finst die could be appeared 5 and the second die could be appeared 3 , or the other possibility.
Then, give an example in tossing a die.
But, before tossing a die, ask one of students to predict what number will be appear?

## b. Main activities

$\mathbf{2}^{\text {nd }}$ phase: Clarify the information.

1. Inform the students about probability of an event and how to determine probability.
2. Inform to students about the learning that will be done, that is Students Team Achievement Division. They will be organized in groups and the score of groups is based on the quiz score of each member in the group.

## $3^{\text {rd }}$ phase: Organizing students in groups.

3. Organize the students into some group consists of 3-5 person.
4. Distribute a worksheet to each group.

## $4^{\text {th }}$ phase: Guiding the groups

5. Ask students to do their worksheet in their group.
6. Give chance to each group to ask if they don't understand about the worksheet.
7. Analyze students' works and give motivation to them.
8. Ask students to write and conclude the result of their group discussion.

## $5^{\text {th }}$ phase: Evaluation

9. Choose some groups to present their group's result in a class discussion.
10. Give opportunity to the other group to comment or ask questions about the presentation.
11. Teacher and students evaluate the presentation and teacher give right answer if there is mistake in students' presentation.

## Giving Individual test (Quiz)

12. Ask students to back in their own chair.
13. Give quiz to the students and ask them to solve individually.
14. Collect the quiz.

## c. Closing

1. Summarize the lesson.

## $6^{\text {th }}$ phase: Giving rewards

2. Give rewards to the best group based on the score group.
3. Give homework.

## Materials and source

## Sources:

- Urban, Paul. 2004. Mathematics for the International Students. Mathematics HL (Core). Australia : Haese and Harris Publication
- http://illuminations.nctm.org/Lessons/ProbExplorations/WhatAre

MyChances-AS.pdf

- http://nrich.maths.org/583
- http://www.mathgoodies.com/lessons/vol6/intro_probability.html

Materials:

- A pair of dice
- 2 packs of cards
- 2 coins


## Assessment

Technique : Written Test
Instrument model : Quiz

## D. Instrument (Quiz)

1. 

A glass jar contains 6 red, 5 green, 8 blue and 3 yellow marbles. If a single marble is chosen at random from the jar, what is the probability of

choosing a red marble? A green marble? A blue marble? A yellow marble?
2.
probability of getting :
a) A sum of 7 or 11
b) A sum greater than 8
3.

A ticket is randomly from a basket containing 3 green, 4 yellow, and 5 blue tickets. Determine the probability of getting :
a. A green ticket
b. An orange ticket
c. A green or yellow ticket
d. A green, yellow, or blue ticket

## E. Scoring Rubric

\begin{tabular}{|c|c|c|}
\hline No. \& Answer \& Score \\
\hline 1. \& \begin{tabular}{l}
The possible outcomes of this experiment are red, green, blue and yellow. \\
There are 22 outcomes: \\
6 red, 5 green, 8 blue and 3 yellow marbles
\[
6+5+8+3=22
\] \\
Probabilities:
\[
\begin{aligned}
P(\text { red }) \& =\frac{\text { the number of ways to choose red }}{\text { the total number of marbles }} \\
\& =\frac{6}{22} \\
\& =\frac{3}{11} \\
P(\text { green }) \& =\frac{\text { the number of ways to choose green }}{\text { the total number of marbles }} \\
\& =\frac{5}{22}
\end{aligned}
\]
\end{tabular} \& 2

7
7 <br>
\hline
\end{tabular}



|  | $\begin{aligned} P(\text { blue }) & =\frac{\text { the number of ways to choose blue }}{\text { the total number of marbles }} \\ & =\frac{8}{22} \\ & =\frac{4}{11} \\ P(\text { yellow }) & =\frac{\text { the number of ways to choose yellow }}{\text { the total number of marbles }} \\ & =\frac{3}{22} \end{aligned}$ | 7 7 |
| :---: | :---: | :---: |
|  | Subtotal scores $=30$ |  |
| 2. | The sample space is : <br> $\{(1,1),(1,2),(1,3),(1,4),(1,5),(1,6),(2,1)$, <br> $(2,2),(2,3),(2,4),(2,5),(2,6),(3,1),(3,2)$, <br> $(3,3),(3,4),(3,5),(3,6),(4,1),(4,2),(4,3)$, <br> $(4,4),(4,5),(4,6),(5,1),(5,2),(5,3),(5,4)$, <br> $(5,5),(5,6),(6,1),(6,2),(6,3),(6,4),(6,5)$, $(6,6)\}$ <br> a. $\quad$ The event of getting a sum of 7 <br> or 11 : <br> $\{(1,6),(2,5),(3,4),(6,1),(5,2),(4,3),(5,6)$, $(6,5)\}$ <br> So, the probability of getting a sum of 7 or 11 is : $P(1 \text { sum of } 7 \text { or } 11)=\frac{8}{36}=\frac{2}{9}$ <br> b. The event of getting a sum greater than 8 : $\begin{aligned} & \{(3,6),(4,5),(4,6),(5,4),(5,5),(5,6),(6,3) \text {, } \\ & (6,4),(6,5),(6,6)\} \\ & \text { So, the probability of getting a sum } \end{aligned}$ | 11 |




## Worksheet

Group
Member of the group :

Date:
Main Material : Probability

Learning Objectives :

1. Students are able to determine experimental probability of an event.
2. Students are able to determine theoretical probability of an event.

## What Are My Chances?

You will be evaluating games of chance to help you understand probability. For each game of chance, predict what will be the most frequent outcome. Then run the experiment 10 times. For each trial, record the actual outcome in the Result row. If
 this matches your predicted outcome, put a check mark in the Prediction row.
1.

Flip a Coin
Prediction for most frequent outcome: Heads Tails

| Result |  |  |  |  |  |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Predictio <br> n |  |  |  |  |  |  |  |  |  |  |


2.

Roll 1 Die
Prediction for most frequent outcome: 123456

| Result |  |  |  |  |  |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Predictio <br> n |  |  |  |  |  |  |  |  |  |  |

3. 

Pick a Card Color
Prediction for most frequent outcome: Red Black

| Result |  |  |  |  |  |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Predictio <br> n |  |  |  |  |  |  |  |  |  |  |

4. 

Pick a Card Suit
Prediction for most frequent outcome: Clubs (a) Spades (a) Diamonds ( $\uparrow$ ) Hearts ( $\uparrow$ )

| Result |  |  |  |  |  |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Predictio <br> n |  |  |  |  |  |  |  |  |  |  |

5. Pick an Exact Card

Prediction for most frequent outcome: $\qquad$ (e.g., 3-)

| Result |  |  |  |  |  |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Predictio <br> n |  |  |  |  |  |  |  |  |  |  |

6. 

In which game of chance were your predictions most accurate?
7. Complete the table below with the probability for each event. Use the results from your experiments above to calculate the experimental probabilities.

| Game of | Event | Experimenta | Theoretical |
| :--- | :--- | :--- | :--- |


| Chance |  | I Probability | Probability |
| :---: | :---: | :---: | :---: |
| Flip a Coin | Heads |  |  |
| Roll 1 die | 6 |  |  |
| Pick a Card <br> Color | Red |  |  |
| Pick a Card Suit | Diamonds |  |  |
| Pick an Exact <br> Card | 5 of <br> diamonds |  |  |

8. 

Compare the theoretical and experimental probabilities for each game of chance.
9. Collect data from the entire class for the probability of an event matching the predicted event (Note: This works even if different groups predicted different outcomes.) Record the number of correctly predicted trials and the experimental probability of each. Since each group performed 10 trials for each game, the number of trials will be $10 \times$ the number of groups.

| Game of <br> Chance | The Number of <br> Correct <br> Predictions | Experimental <br> Probability |
| :---: | :---: | :---: |
| Flip a Coin |  |  |
| Roll 1 die |  |  |
| Pick a Card <br> Color |  |  |
| Pick a Card Suit |  |  |
| Pick an Exact <br> Card |  |  |

10. Are the experimental probabilities different in Questions 7 and 9 ? Why or why not?
11. How do the theoretical probabilities in Question 7 compare to the experimental probabilities in Question 9? What do you think would happen if even more trials were added?

## Assessment Rubric

Group:

| Member of The <br> Group |  |  |  |  |  |  | Total |
| :---: | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
|  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |
| Total Score of <br> Group |  |  |  |  |  |  |  |
| Average Score <br> of Group |  |  |  |  |  |  |  |
| Reward |  |  |  |  |  |  |  |


| Name of <br> the <br> Students | Date: 10 Mei 2010 |  |  |  | Date: |  |  |
| :---: | :---: | :---: | :---: | :--- | :--- | :--- | :---: |
|  | Quiz : Probability | Quiz: |  |  |  |  |  |
|  | Basic <br> Score | Quiz <br> Score | Developme <br> nt Score | Basic <br> Score | Quiz <br> Score | Development <br> Score |  |
|  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |

Criteria of Development Score

| Perfect Score | 30 points |
| :--- | :---: |
| If the score more than 10 point of basic | 30 points |
| score | 20 points |
| If the score is same as the basic score |  |
| until 10 point more than basic score | 10 points |
| $1-10$ point less than the basic score | 5 points |
| $>10$ points under the basic score |  |



